Induction of T cell memory by a dendritic cell vaccine: a computational model
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ABSTRACT

Motivation: While results from phase III clinical trials substantially support the use of prophylactic and therapeutic vaccines against cancer, what has yet to be defined is how many and how frequent boosts are needed to sustain a long lasting and protecting memory T cell response against tumor antigens. Common experience is that such preclinical tests require the sacrifice of a relatively large number of animals, and are particularly time and money consuming.

Results: As a first step to overcome these hurdles, we have developed an ordinary differential equation model that includes all relevant entities (such as activated cytotoxic T lymphocytes and memory T cells), and investigated the induction of immunological memory in the context of wild type mice injected with a dendritic cell-based vaccine. We have simulated the biological behavior both in the presence and in the absence of memory T cells. Comparing results of ex vivo and in silico experiments, we show that the model is able to envisage the expansion and persistence of antigen-specific memory T cells. The model might be applicable to more complex vaccination schedules and substantially in any biological condition of prime-boosting.

Availability: The model is fully described in the article.
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1 INTRODUCTION

In the last years both therapeutic and preventive vaccines have been developed with the aim to fight and prevent different types of cancers (Kantoff, 2010; Kenter et al., 2009; Kahn, 2009). The power of vaccines relies on their ability to stimulate a strong and long-lasting antigen-specific immune response, mediated both by B and T lymphocytes. While induction of a protective titer of neutralizing antibodies is the main objective of most of the vaccines against infectious agents, including vaccines to carcinogenic human papillomavirus (HPV) and hepatitis B virus (HBV), which also protect from cervical and liver cancer, respectively (Lollini et al., 2011), evidence in humans that antibodies induced by a vaccine can contribute to antitumor immunity is scanty (Schoenfeld et al., 2010). Conversely, the major goal of both prophylactic and therapeutic vaccines against non-infectious tumors, which account for approximately 80% of all tumors (Lollini et al., 2011), is to induce a long-lasting antigen-specific CD8 T cell immunity. In support of this concept, high densities of effector memory CD8+ cytotoxic T cells are associated with a longer overall survival in several human cancers (Fridman et al., 2012).

Usually, an effective vaccine, requires multiple immunizations in the form of prime-boost. Several studies have shown that boosting with a different vector carrying the same antigen is better at enhancing immune responses than boosting with the homologous vector. The mechanism underlying this phenomenon is still obscure. Heterologous prime-boost approaches are now widely used in efforts to develop vaccines (Kaufmann, 2010; Sallusto et al., 2010). It is also generally accepted that a strong primary immune response is required to give rise to a large pool of memory cells (Sprent and Surh, 2011). However, what affects the longevity of memory T cells is not fully understood, and much controversy exists regarding the role of antigens in this process (Zinkernagel, 2002; Sprent and Surh, 2011; Kaeche et al., 2002). Indeed, sustained high amounts of soluble antigens often lead to tolerance or exhaustion both in T and B cells. As a result of exhaustion, antigen-specific T and B cells express a variety of inhibitory receptors such as PD-1, LAG-3, CD244, CD160, TIM-3 and CTLA-4 (Wherry, 2011).

Dendritic cell (DC)-based vaccines have been extensively investigated as potential cancer therapeutic vaccines because of the primary role of DCs as antigen presenting cells (APCs) and their unique ability in T cell priming (Banchereau and Steinman, 1998). Indeed, DCs pulsed with the antigen of choice induce a potent antigen-specific immune response and favor the generation of the memory pool. This stems from the asymmetric division of engaged naive T cells into effector and memory cells (Chang et al., 2007). Several phase II clinical trials based on the use of DCs pulsed with tumor associated antigens are ongoing (Finn, 2008). Moreover, Sipuleucel-T (Provenge; Dendreon, Inc.), an autologous APC-based vaccine has been the first vaccine approved by the Food and Drug Administration for the treatment of cancer patients. In
a phase III trial in patients affected by castration-resistant prostate cancer Sipuleucel-T gave a 4.1-month benefit in overall survival relative to a control arm that received unpulsed APCs. However, no significant effects on the time to objective disease progression were observed (Kantoff, 2010). These promising results also suggest that some fundamental biological questions remain unanswered. Indeed, for DC-based vaccines it is not yet known whether booster immunizations should consist of DCs or other means. It has been reported that antigen-bearing DCs are rapidly eliminated by antigen-specific cytotoxic T lymphocytes (CTLs) when injected in previously vaccinated mice (Yang et al., 2006; Guarda et al., 2007), therefore arguing for a reduced effectiveness of DC-based boosts. Jouanneau et colleagues observed in the GL26 model that DCs are essential for the priming, but they are less effective than tumor cell lysate alone in boosting the anti-tumor immune response and for the induction of long-term immune memory (Jouanneau et al., 2006). Another unsolved issue is the frequency of boosting. Indeed, it has been reported that repeated immunizations result in increased frequencies of memory T cells (Masopust et al., 2006; Wirth et al., 2010). However, over stimulation can drive memory T cells toward terminal differentiation such as activation-induced cell death, fratricide, or exhaustion (Overtijk and Restifo, 2001; Wherry, 2011).

To address these biological issues, we started analyzing the ability of DC-based vaccines to induce a long-lasting antigen specific immune response in mice. As immunological readout of antigen-primed and functional T cells, we measured the interferon gamma (IFN-γ) contained in sera of vaccinated mice, and the frequency of CD8$^+$CD44$^+$ T cells able to release IFN-γ upon ex vivo specific antigen challenge (Camporeale et al., 2003). Preliminary experiments suggested that to optimize the best boosting strategy we would have had to set many experiments each lasting several months. To investigate these biological problems, as a first step, we began by setting up an in silico model capable to describe the biological phenomena observed in the animal model. The aim of the model is to verify the memory T cell induction hypothesis by a DC-based vaccine observed in vivo, and to give new suggestions on the designing of boosting strategies. During the last decades, several approaches have been devoted to model the immune system or parts of it, with mathematical equation-based models representing the largest slice among these approaches. Differential equation based models usually reproduce the dynamics of the average concentrations of the immune system involved entities over time, to obtain the main aspects of the immune response. Simple models based on systems of ordinary or partial differential equations can be easily analyzed to obtain, for example, asymptotic behaviors. On the other hand, for more complex scenarios, it is usually difficult to build complex ordinary differential equations (ODE) based models as well as incorporate new aspects. The trade-off between an accurate biological representation and the mathematical feasibility may lead to biologically useless models or to mathematically intractable models.

Cellular automata (CA) or agent-based models (ABM) represent a large class of discrete modeling techniques where each entity is followed individually, and global behaviors are obtained from local behaviors of all involved entities. In this way it is possible to model the immune system in much more details, allowing to determine behavior distribution (and not just the average). Moreover it is very easy to add and remove new entities and nonlinear interactions, in order to expand or update the model to the last biological insights, leaving the problem computationally tractable. CA and ABM can be successfully used to simulate without any problems the receptor diversity of the immune repertoire, opening the door to natural scale simulations. An example of approaches in this direction are discussed in (Halling-Brown et al., 2010). However, even such approaches have their own flaws: due to the lack of a solid mathematical theory, they miss tools allowing any asymptotic analysis, and require considerable computational power to simulate individual agents, in particular for large scale simulations. Some good review articles that can introduce the reader to the modeling techniques of the immune system are presented in (Perelson and Weisbuch, 1997; Ludengaard et al., 2007; Germain et al., 2011).

The problem we are dealing with requires the ability to uniquely represent the immune response of CTLs specific for the immunodominant Tag-IV antigen from the oncovirus SV40 (Mylin et al., 1995), (and also in vivo measurements refer to this). This is a valid argument for supporting the assumption that a monoclonal model based on ODE described in this paper can be considered adequate. The (ODE) model includes all the relevant entities (such as activated CTLs and memory T cells) needed to confirm the presence of immunological memory. We simulated the biological behavior in the presence and in the absence of memory T cells.

2 METHODS

2.1 Model description

In order to model antigen-specific CTL activation and differentiation into memory T cells upon vaccination with pulsed DCs, we developed a model based on a system of 6 ODEs for 6 different populations: pulsed DCs ($D_1$) in the injection point, pulsed DCs ($D_p$) in the presenting locations, naive CTLs ($T_n$), activated CTLs ($T_a$), memory T cells ($T_m$) and IFN-γ ($I$).

Equations 1 and 2 deal with the pulsed DCs at the injection point and the presenting location, respectively. These two equations are used to model the injection of pulsed DCs into the host and their consecutive migration from the injection point to the site where presentation to CTLs occurs (i.e. lymph nodes). $D_1$ (eqn. 1) are injected according to the function $k_{in}(t,q)$ that introduces into the system $q$ pulsed DCs if, according to the administration protocol, at time $t$ an injection is scheduled. $D_1$ then migrate to presenting locations (term $-\alpha_{50} D_1$). They can also disappear from natural death (term $-\alpha_1 D_1$).

\[
\frac{dD_1}{dt} = k_{in}(t,q) - \alpha_{50} D_1 - \alpha_1 D_1
\]

(1)

Equation 2 models the behavior of pulsed DCs into the presenting location. $D_p$ are estimated on the basis of migrating $D_1$ (term $\alpha_{50} D_1$) and disappear from the system for multiple causes, such as natural death (term $-\alpha_1 D_p$).

\[
\frac{dD_p}{dt} = \alpha_{50} D_1 - \alpha_1 D_p
\]

(2)

We initially considered the possibility to model the migration process using delay differential equations, by adding in eqn 2 (term $\alpha_{50} D_1$) a time delay of approximately 2-4 hours. However, we abandoned this approach because after some numerical simulations we noted only negligible differences between results obtained with and without time delay. This is probably due to the fact that such a short time delay becomes insignificant in respect to the time-scale of the experiment (1 year).

Equation 3 models the antigen-specific naive CTLs behavior ($T_n$). In general when naive CTLs are activated, they are replaced by means of
haematopoiesis to keep the naive CTLs number almost constant as specified in the leukocyte formula. Of course, this does not mean that the newborn CTLs will share the same MHC/antigen complex specificity of previously activated cells. Present immunological knowledge cannot predict if and when a CTL will be replaced by one of the same specificity. Moreover, cells receptor are randomly selected by DNA recombinations. Hence, it is feasible to suppose that after a reasonable time window, the level of antigen-specific CTLs will approach to the same initial level. Finally, this is in line with the fact that the immunological repertoire is almost specific for each individual.

The term $h_1(T_{n0} - T_n)$ represents the recovery rate. Under safe conditions (absence of the pathogen) the number of T cells tends to a given value $T_{n0}$. When antigenic presentation by $D_p$ occurs naive T cells are activated (term $-a_5 D_p T_n$). We note here that equation 3 takes into account only a small portion of naive T cells population composed by those cells whose receptor is able to recognize the specific antigen, and not the entire T cells population.

$$\frac{dT_a}{dt} = h_1(T_{n0} - T_a) - a_5 D_p T_a \quad (3)$$

Activated CTLs ($T_a$) are modeled by equation 4. They appear in the system as a consequence of the antigenic presentation to $T_n$ by $D_p$ cells (term $-a_5 D_p T_n$) and can disappear from the system due to death ($-a_3 T_a$).

As a consequence of activation, a small portion of activated T cells can become memory cells ($-a_20 T_a$).

$$\frac{dT_a}{dt} = a_5 D_p T_n - a_20 T_a - a_3 T_a \quad (4)$$

Memory CTLs (eqn. 5) are estimated on the basis of activated T cells (term $a_20 T_n$) and then disappear from the model due to multiple causes, among which natural death ($-a_21 T_n$).

$$\frac{dT_m}{dt} = a_20 T_n - a_21 T_n \quad (5)$$

The last equation (eqn. 6) describes IFN-γ dynamics. The quantity of IFN-γ released by CTLs is taken as outcome of the ex vivo experiment and it is used to estimate the number of activated T cells. In order to compare our results with ex vivo observation we modeled IFN-γ dynamics as follows. IFN-γ is released by activated and memory T cells, which are supposed to release the same quantity of IFN-γ (term $h_{10}(T_m + T_n)$), and disappear from the model for natural degradation (term $-\alpha_{10} I$).

$$\frac{dI}{dt} = h_{10}(T_m + T_n) - \alpha_{10} I \quad (6)$$

It is worth mentioning here that the capacity to endow the host with the ability to learn through multiple encounters, and then generate memory, is in general not representable by ODEs. This important aspect has been analyzed using, for example, agent based modeling (Palladini et al., 2010; Pennisi et al., 2010). We modeled the learning phase that arises from the multiple encounters of T cells with targets cells by coding that into coefficients that were tuned in order to reproduce the fraction of memory T cells generated and observed in the mouse: the memory is then represented as the activation of dormant pathways.

Parameter values are shown in Table 1 and have been set at reasonable values based on results coming from the literature, from the observation of the in vivo experiments and from our past experience (Pappalardo et al., 2009b; Pennisi et al., 2008; Halling-Brown et al., 2010; Pappalardo et al., 2010; Pennisi et al., 2009; Castiglione et al., 2012; Pappalardo et al., 2011, 2012, 2006, 2009a).

Numerical simulations start at week 8 ($t_0 = 0$), time of the first injection of pulsed DCs. The time-length of the simulations has been set to 360 days. The physical time step for the simulations is $\Delta t(1) = 1$ day. To solve numerically the ODE system we used Berkeley Madonna software. Initial conditions have been set to 0 for all populations except for $T_n$ where $T_n(0) = T_{n0}$. Since Tag-IV is an antigen specifically designed to give rise to a very strong immune response, we supposed that approximately 20% of the total population of naive CTLs was potentially able to recognize the antigen. Supposing a total population of approximately 400 naive CD8 T cells per mm$^3$, we set up $T_{n0} = 80$. The differentiation rate of activated CTLs ($a_{20}$) has been tuned up in such a way that the total number of newborn memory T cells for each injection of pulsed DCs is approximately around the 5% of the maximum number of activated T cells for each injection. Moreover to simulate lack of memory $a_{20}$ has been set to 0. The parameters that we defined as “tuned” are free parameters, i.e. they were set in order to fit the experimental data. We highlight here that for these parameters there are no measures in the literature.

It’s worth noting that we used the levels and the proportions of IFN-γ+ cells and KI/Tag+ cells at week 9 to calibrate the model and the same levels and proportions at week 18 to validate the model results.

### 2.2 LHS-PRCC sensitivity Analysis

In order to understand which parameter may be considered fundamental in this process, it is important to analyze the sensitivity of the model to variation of parameters. Classical sensitivity analysis is usually done by varying a given parameter in reasonable ranges and keeping the others constant. Obviously results coming from this kind of analysis are strongly bound to the values of the fixed parameters and different sets of values for the fixed parameters may lead to completely different results.

Partial rank correlated coefficients (PRCC) (Saltelli, 2004) is a statistical sensitivity analysis technique which tries to overcome the limits of classical sensitivity analysis by computing a partial correlation on rank-transformed data between two sets of variables, represented in our case by the model input parameters and the model entities values. The strength of such a methodology is given by the fact that correlation does not depend by a given set of parameters, and it is therefore possible to estimate how variations in a given parameter may influence the results of the model, despite the value of the other parameters. Nevertheless the methodology can be in principle easily applied and used with any kind of continuous or discrete model.

The methodology we used to perform sensitivity analysis (LHS-PRCC) is briefly described as follows. More information about this methodology can be found in (Marino et al., 2008). Parameters space is initially sampled

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Table 1. ODE model parameters. $q$ represents the number of injected pulsed DCs / ml; it was tuned with in vivo results. $a_1$ is the pulsed DCs death rate (half-life $\sim 7$ days) (Mered and Manz, 2009). $a_{50}$ is the migration rate of $D_i$ towards presentation location; it was tuned. $h_1$ is the T naive cells recover rate; it was tuned. $a_5$ is the CTL activation rate; it was tuned.$a_{23}$ is the activated T cell death rate (half-life $\sim 2$ days) (DeBoer et al., 2003). $a_{20}$ is the memory T cell differentiation rate; it was tuned. $a_{21}$ is the memory T cell death rate (half-life 8 weeks); it was tuned. $h_{10}$ is the IFN-γ quantity released by T cells (fg/ml) (Pennisi et al., 2010). $a_{10}$ is the IFN-γ degradation rate (half-life $\sim 9$ hours).
using a Monte-Carlo technique. In this case we use a technique named Latin-Hypercube-Sampling (LHS) (Mckay et al., 1979). The technique divides the random parameter distributions into \( N \) (where \( N \) represents the chosen sample size) equal probability intervals that are then sampled. The choice for \( N \) should be at least \( k+1 \), where \( k \) is the number of parameters varied, but usually much larger to ensure accuracy. In our trials we set \( N = 1000 \).

After sampling, a LHS matrix \( X \) of sampled parameters is built. Each row represents a unique set of variables for the model sampled without replacement.

The model is then solved for each row of \( X \), and the model output values are stored into an output matrix \( Y \). Each matrix is then rank-transformed (\( X_R \) and \( Y_R \)). \( X \) and \( Y \) can be used to calculate the Pearson correlation coefficient. \( X_R \) and \( Y_R \) can be used to calculate the Spearman or rank correlation coefficient (RCC) and the partial rank correlation coefficient (PRCC).

PRCC between an input parameter \( x_j \in X_R \), \( j \leq k \) and output \( y \in Y_R \) is then computed by considering the residuals \( x_j - \hat{x}_j \) and \( y - \hat{y} \), where \( \hat{x}_j \) and \( \hat{y} \) are given by the following regression models:

\[
\hat{x}_j = c_0 + \sum_{p=1,p \neq j}^{k} c_p x_p \quad \text{and} \quad \hat{y} = b_0 + \sum_{p=1,p \neq j}^{k} b_p x_p
\]

Using this methodology we analyzed the effects of the most important input parameters which most influence the behaviour of the released IFN-\( \gamma \).

2.8 Statistical analysis of in vivo experimental studies

Prism 5.0a software was implemented to conduct statistical analysis on data collected in ex vivo immunological assays. Comparison of data collected from the different experimental groups of mice (at least 5 mice/group) was conducted using the ANOVA, and Newman-Keuls or the two-tailed Students t test tests. Values were considered statistically significant for \( P < 0.05 \).

2.9 Measurements for in silico setup

In order to set up the in silico approach we measured the induction and maintenance of an antigen-specific CTL response in C57BL/6 mice injected with DCs pulsed with Tag-IV, the immunodominant CTL epitope from the SV40 Tag antigen (DC-Tag) (Mylin et al., 1995).

2.10 Ethics Statement

Wild type C57BL/6 mice (Charles River Breeding Laboratories; Calco, IT) were housed in a pathogen-free animal facility, and treated in accordance with the European Community guidelines. The in vivo experiments were approved by the Ethical Committee of the Istituto Scientifico San Raffaele (IACUC # 410).

3 RESULTS AND DISCUSSION

3.1 The biological experiment

Eight-week-old mice were primed with a single i.d. injection of DC-Tag, and a first group was sacrificed one week later (Figure 1A). A substantial amount of CD8\(^+\)CD44\(^+\) T cells were found in the spleen of vaccinated mice that bound K\(^b\)/Tag pentamers (Figure 1B), therefore demonstrating to be antigen-experienced and specific for Tag. Among the Tag-specific T cells, almost 80% displayed an effector phenotype (i.e. CD62L\(^-\)), whereas more than 20% were central memory (Figure 1C). We investigated if the IFN-\( \gamma \) measured in the sera of vaccinated mice could be used as an indicator of the effector function of antigen-specific CD8\(^+\) T cells. Indeed, the amount of IFN-\( \gamma \) in the sera of vaccinated mice one week after priming was more than 3-fold the amount found in naive littersmates (56.3 \( \pm \) 10.8 vs 17.2 \( \pm \) 2.5 pg/ml, respectively). However, this value remained stable thereafter, and did not mimic the drop in Tag-specific T cells found by pentamer staining at week 18 (Figure 1B and data not shown). This was likely due to the fact that several cells of the innate and adaptive arms of the immune system concur in producing IFN-\( \gamma \) upon vaccination. Thus, we utilized an ex vivo intracellular production assay to investigate the effector function of antigen-specific T cells activated by vaccination. Interestingly, a fraction of CD8\(^+\)/CD44\(^+\) T cells similar to that found with K\(^b\) pentamer staining (Figure 1B) also produced IFN-\( \gamma \).
upon antigen-specific challenge (Figure 1D) and specifically killed targets expressing the relevant antigen (data not shown), therefore confirming our previously published data (Rigamonti et al., 2011). To investigate the effects of boosts on the dimension of the antigen-specific memory pool, mice were boosted with DC-Tag 4 weeks later. This time schedule was chosen based on the notion that an ideal memory CTL response requires 4-6 weeks to settle in (Sallusto et al., 2010). In spite of the recent vaccination, one week after the first boost the percentage (Figure 1D) and number (Figure 1F) of CD8⁺CD44⁺ T cells producing IFN-γ substantially decreased. Mice were boosted 6 weeks later, and the last group of mice was sacrificed 6 weeks after the third boost (Figure 1A). As expected from a memory response measured more than a month after immunization (Wirth et al., 2010), the number of Tag-specific splenocytes dropped of almost one log (Figure 1B), whereas central memory T cells increased (Figure 1C). A similar proportion between effector and memory T cells was found within the population of IFN-γ⁺ cells (Figure 1E), therefore suggesting that K⁵/Tag and IFN-γ stained the same cells. Interestingly, both the 1D) and the absolute number (Figure 1F) of antigen-specific CTL remained stable thereafter, therefore suggesting that the vaccination procedure allowed the induction of a long-lasting antigen-specific memory response.

3.2 The in silico experiment

In order to model CTL activation and differentiation into memory T cells upon vaccination with pulsed DCs, we developed a model based on a system of 6 ODEs for 6 different populations (for details see Materials and Methods section).

3.2.1 Supporting long last T memory hypothesis. In Figure 2 we show the ODE immune system behavior for the following entities: DC-Tag in the injection point and where the antigen is presented (D₀ and Dₚ, respectively), naive, activated and memory antigen specific CTLs (Tₐ, Tₕ, and Tₘ), and the levels of IFN-γ released by antigen-specific CTLs (I), starting from week 8 for a period of one year. To compare ex vivo results with the in silico experiments, we evaluated the total number of activated and memory CD8⁺ T cells and their percentage measured at week 9 and 18 (Figures 3 and 4). Figure 3 shows the total number of Tag⁺ T cells (both activated and memory specific CTLs) at weeks 9 and 18. Comparing these results with Figure 1B one can notice that the model qualitatively reproduces the same proportions observed ex-vivo. Moreover, looking at Figure 4 the percentage of specific memory CTLs follows the same dynamics observed ex-vivo in Figure 1C. These results are in good agreement with the ex vivo data, and all together support the immunological memory hypothesis.

3.2.2 Prediction of the role of the second injection (Boosting) over the pool of memory T cells. To both investigate the role of the second injection (boosting) over the pool of memory Tag-specific CTLs, and to verify the prediction capabilities of the mathematical model, we simulated two scenarios. In these simulations we executed, as in previous experiments, the first priming with DC-Tag at week 8. This priming was followed (or not) by a second injection of DC-Tag at week 12 (boost). The outcome of the experiment was represented by the number of specific CTLs (Tₜ + Tₘ) at week 9, and at week 18 both in presence and absence of the boosting. The
simulations showed a lower level of specific memory CTLs in the absence of the boosting (see Figure 5).

A similar experiment was then set-up in vivo, where the mice were primed at week 8 by DC-Tag. The initial set of mice was divided in three groups. The first group was sacrificed at week 9 (priming) to measure primary response. The second and third groups where left untouched (no boost) or boosted at week 12 with DC-Tag (priming) to measure primary response. The second and third groups were primed at week 8 by DC-Tag. The initial set of mice was divided in three groups. The first group was sacrificed at week 9 and 18. Percentages are in a good agreement with the ex vivo results (see Figure 1C).

Fig. 5. Importance of the second injection over the pool of memory CTLs predicted by the mathematical model (in silico) and confirmed by the in vivo experiment (animal model). (A) Schematic representation of the experiment. Eight-week-old C57BL/6 mice were primed by i.d. injection of DC-Tag and either killed one week later (week 9, n=5) or boosted (Boost, n=13) or not (No Boost, n=13) 4 weeks later, and sacrificed 10 weeks after priming (week 18). (B) For the in silico experiment the number of specific memory CTLs (Tm + Ta) at week 9, and at week 18 both in presence and absence of the boosting were taken into account; For the in vivo experiments, the effector function of Tag-specific CD8+ T cells was assessed ex vivo by flow cytometry analysis of intracellular IFN-γ production in the presence of Tag-IV. Percentage of IFN-γ+ producing cells are depicted following electronic gating on CD8+CD44+ viable cells. (Data are representative of at least 3 independent experiments. Statistical analyses were done using the Student’s T test tests. **: 0.001 < p < 0.01.

3.3 LHS-PRCC Sensitivity analysis

Since activated CTLs release IFN-γ, we tracked, using partial rank correlation coefficient (PRCC) analysis, the effects of the model
parameters on the quantity of the released cytokine. It’s worth mentioning here, that the results of the analysis we performed are strictly dependent on the 4-injections vaccination schedule we have modeled. Results of sensitivity analysis are available as Supplementary data S1. Here we only outline the major findings.

3.3.1 Role of CTL differentiation and death rates over IFN-γ. Sensitivity analysis reported that memory CTL differentiation rate coefficient $a_{20}$, which gives an estimation of the rate of activated CTLs ($T_m$) that differentiate into memory cells ($T_n$), showed a reduced correlation with IFN-γ, especially shortly after every DC-Tag, whereas a correlation increased with the distance from the vaccine injection. This can be explained by the fact that after every injection, the immune response is mainly mediated by activated CTLs, whereas memory CTLs cells give a minor contribution at this time, especially after the first two injections. Far from injections, the immune response of activated CTLs declines and memory CTLs become the principal cells involved in IFN-γ release. Similar considerations also hold when we verified the impact of memory CTL death rate on IFN-γ.

3.3.2 Role of naive CTL recovery rate over IFN-γ. The naive cell recovery rate ($h_1$), which refers to the speed at which the immune system reconstitutes the naive CTLs pool with newly generated CTLs, showed almost no correlation between the naive cell recovery rate and the IFN-γ production, except for a short period of time around week 12, just after the second injection of DCs. At that time the number of $T_n$ was lower than those related to the other administrations. It is worth noting that higher values of $h_1$ would entitle faster recruitment of specific naive CTLs and would allow higher levels of IFN-γ. However such a parameter cannot be modified in vivo. The presence of a positive PRCC correlation when the number of $T_n$ is low may suggest that the second injection of vaccine is given too early, and it should be advisable to delay the second injection in order to give more time to the immune system to repopulate the specific naive CTLs population until no correlation is reached. Lack of correlation for the entire period may in fact represent an important achievement in designing a treatment that is effective not only for an individual, but for an entire population since small variations in the rate of recovery of naive cells for different individuals would not influence the efficacy of the treatment.

4 CONCLUSION

Our in silico model showed the ability to predict the dimension of the immune response induced in mice by DC vaccination, and allowed us to define the relative contribution of several parameters (i.e., memory cell differentiation and death rates and naive cell recovery rate) to the success of the prime-boost strategy. It also predicted the role of the second injection (Boost) over the pool of memory T cells. Nevertheless, it allowed the identification of a time window in which boosts may be detrimental (see Supplementary Data S1 for details). These findings appears to be consistent with data reported by us (Ricupito et al., 2013a) and (Kaech et al., 2002). We have demonstrated that boosting healthy mice every two weeks instead of every month hindered persistence of IFN-γ competent memory CD8+ T cells (Ricupito et al., 2013a). In addition, when vaccinated mice were challenged with melanoma cells, 80% of the mice that had received a monthly boosting rejected the tumor. Conversely, mice treated with tighter vaccination schedules survived similarly to non boosted mice and remarkably less than mice boosted every month (Ricupito et al., 2013b). One of the advantages of the system is that several entities and variables can be added each time. As an example, it might be interesting to investigate the role of endogenous DCs and the antigen formulation (e.g. synthetic peptide, protein or cell fragment) in T cell priming induced by the vaccine. It has been reported that the requirement of antigen transfer to endogenous APCs for in vivo CTL priming by DC-based vaccines may depend on the antigen formulation (Yewdall et al., 2010). Furthermore, by adding the characteristic of the patient (e.g. age, sex, weight, general health status, stage of cancer, comorbidities, medications) a personalized vaccination schedule might be generated. One limit of the reported data is that they were obtained modeling a healthy subject, and therefore they are applicable only for the design of preventive vaccines. The system needs to be challenged against more stringent biological contexts such as in the presence of minimal residual disease or bulky tumors. Our recent findings suggest that tumor antigens released from the tumor as a consequence of either the tumor cell turnover or the immune attack already boost memory T cells induced by vaccine priming, and vaccine boosts may be detrimental. On the other hand, the model does not take into account the regulation of T cell longevity and the peculiarities of the antigens. These issues appear important and future version of the model could incorporate them, as wet experiments reveal their roles.

An additional limit of the study is that it is entirely based on mouse data. Indeed, there are no published clinical trials in which different vaccination schedules have been compared for induction of long-lasting antitumor immunity. Most of the vaccination protocols tested so far in cancer patients stemmed from the experience with prophylactic vaccines against infectious diseases, which are dissimilar to non-infectious tumors. Thus, reliable pre-clinical models are needed to investigate the therapeutic efficacy of cancer vaccines. Mice are the experimental tool of choice for the majority of tumor immunologists, because of the remarkable similarities between mouse and human immune system. Nevertheless, significant differences exist between mice and humans in immune system development, cell subpopulations of both the innate and adaptive arms, and perception of endogenous and exogenous activation signals (Mestas and Hughes, 2004). This should sound a word of caution to avoid over interpreting results obtained in mouse models.

Due to the fact that information is also available for humans on the 6 different populations we used to develop the related ODEs, our model might be easily tested in the human context, and provide useful information for DC-based cancer vaccines.

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