

# COMPARING DRAG REDUCTION TECHNIQUES IN THE "MONEY-VS-TIME" FRAMEWORK

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# OUTLINE

## Background

Money vs  
Time

CPI

## 1 BACKGROUND

## 2 MONEY VS TIME

## 3 CPI

# BACKGROUND

## Background

Money vs  
Time

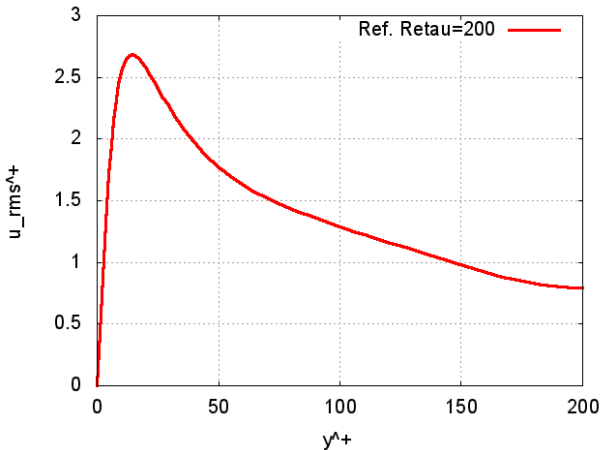
CPI

- Turbulent skin-friction drag reduction
- Open-loop **spanwise** forcing (oscillating wall, travelling waves)

# MOTIVATION

BETTER UNDERSTANDING OF THE PHYSICS

SOW: "Turbulence intensity is destroyed"



Background

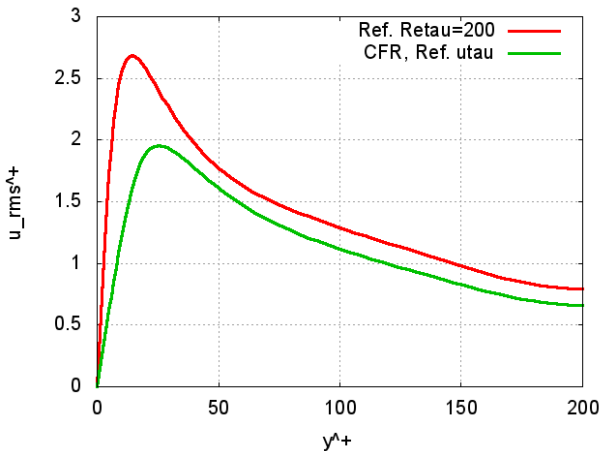
Money vs Time

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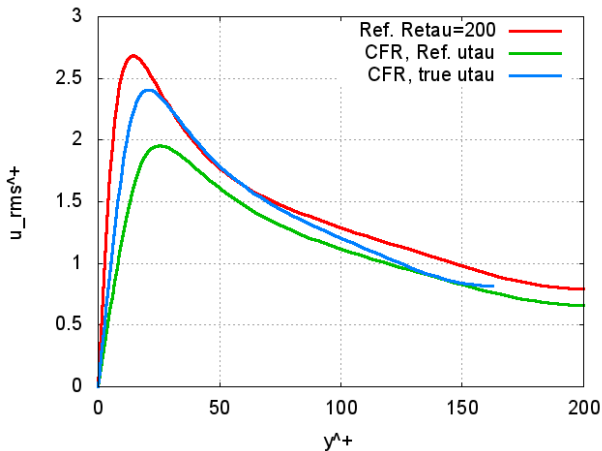
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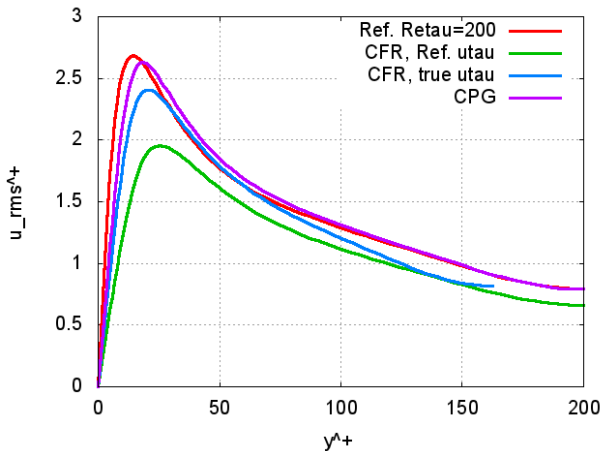
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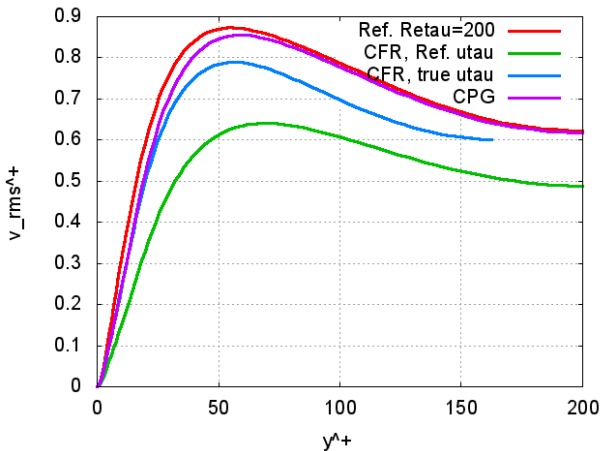
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# MOTIVATION

OTHER COMPONENTS AND/OR DIFFERENT SCALING



Background

Money vs  
Time

CPI



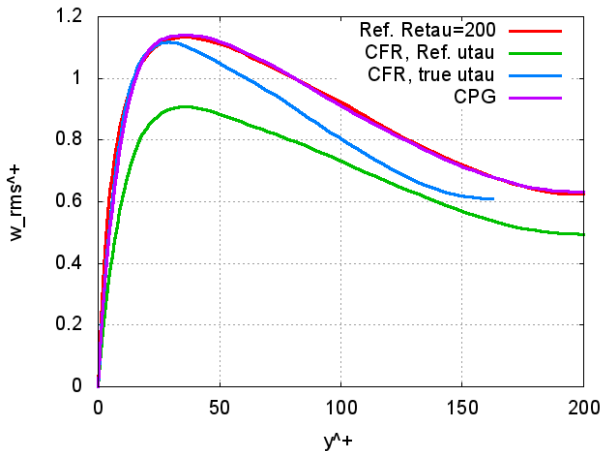
# MOTIVATION

## OTHER COMPONENTS AND/OR DIFFERENT SCALING

Background

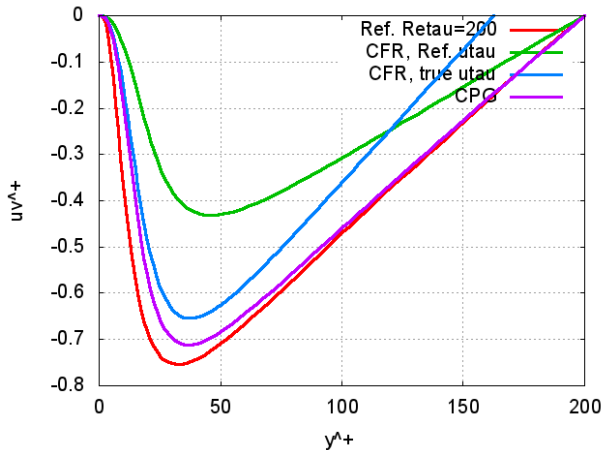
Money vs  
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# MOTIVATION

OTHER COMPONENTS AND/OR DIFFERENT SCALING



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# CONSTANT FLOW RATE OR CONSTANT PRESSURE GRADIENT?

## Background

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- One potential source of confusion
- Concerns both DNS and experiments
- CFR: pumping power is **reduced**
- CPG: pumping power is **increased**

# OUTLINE

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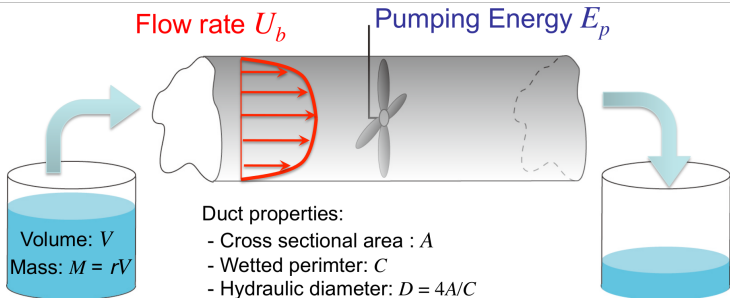
**1** BACKGROUND

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# RE-STATE THE PROBLEM

## Problem setup (dimensional) for duct flows



✓ Fluid travel time per unit length:  $1/U_b$

✓ Pumping energy per unit wetted area:

$$E_p = \frac{\tau_w V}{A} = \frac{MU_b^2 C_f}{2A}$$

Friction coefficient

$$C_f = \frac{\tau_w}{\frac{1}{2}\rho U_b^2}$$

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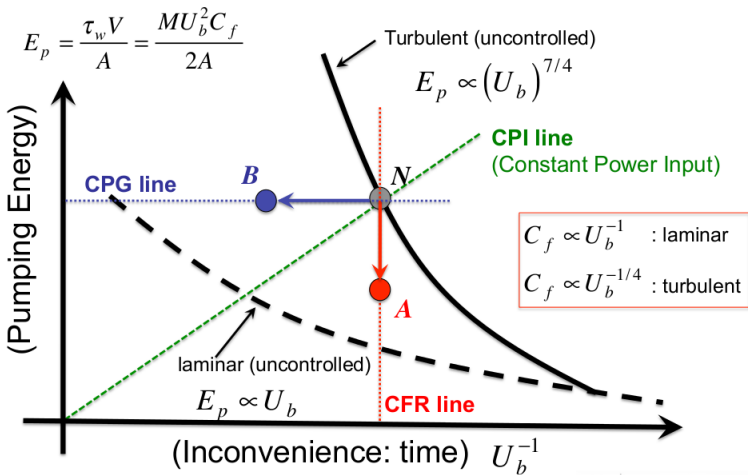
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# ENERGY VS CONVENIENCE

Background

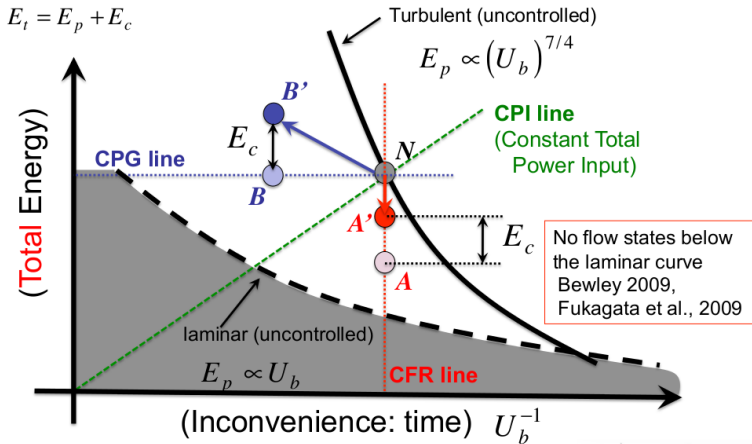
Money vs Time

CPI



# EMPHASIS ON TOTAL ENERGY BUDGET

ADDING CONTROL ENERGY  $E_c$  TO THE PICTURE



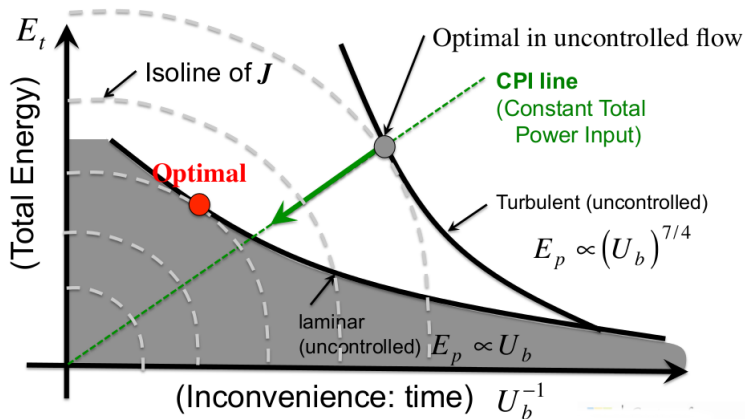
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# COST FUNCTION

$$\text{Cost function: } J = E_t^2 + (1/U_b)^2$$



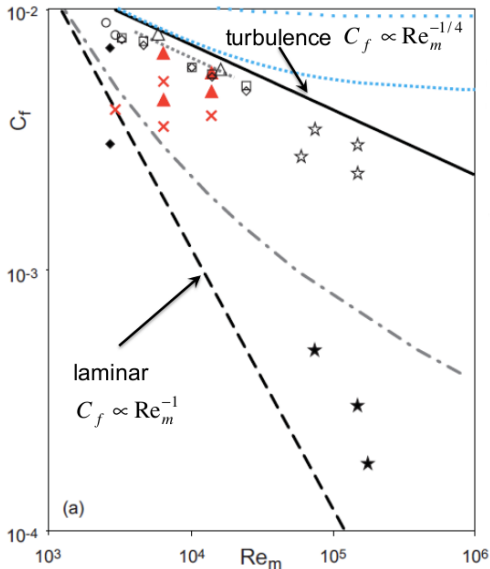
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# THE CONVENTIONAL $C_f - Re$ MAP



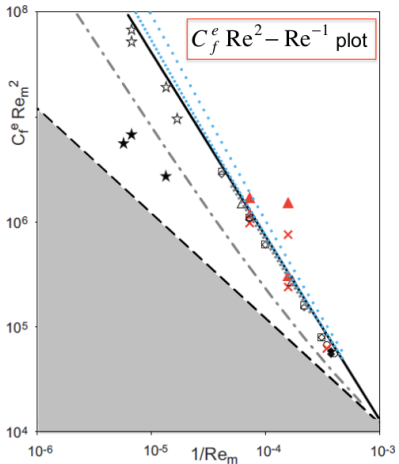
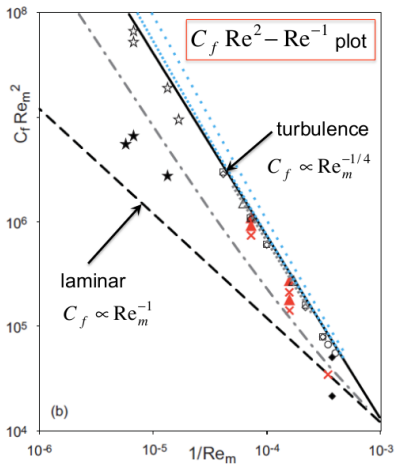
- The value of  $C_f$  does not represent energy consumption
- Comparison of  $C_f$  at different  $Re$  is not meaningful

# THE "MONEY-VS-TIME" DIMENSIONLESS MAP

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# CPI: A USEFUL ALTERNATIVE?

A NATURAL STRATEGY IN THE MONEY-VS-TIME PLANE

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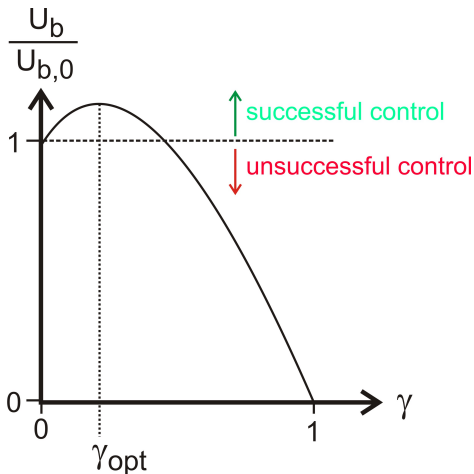
- Total power input is kept constant
- Energy (money) is reduced while flow rate (time) is increased at the same time
- Not "better" (it's application-dependent!)
- May help understanding how turbulence is affected

# WHAT DOES FLOW CONTROL DO IN CPI?

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- $P_t$  = total power
- $\gamma P_t$  = control power
- $(1 - \gamma)P_t$  =  
pumping power

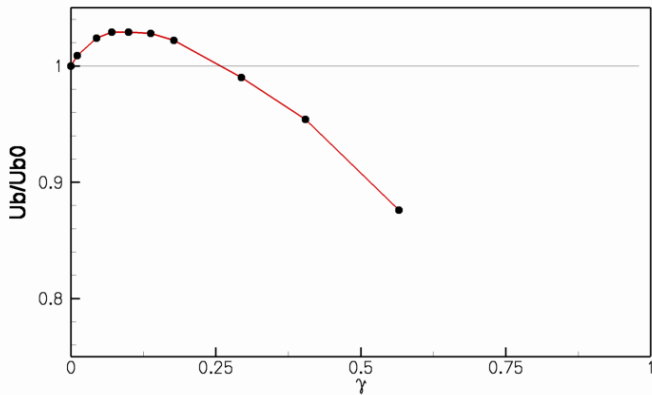
# EXAMPLE RESULTS

## SOW

Background

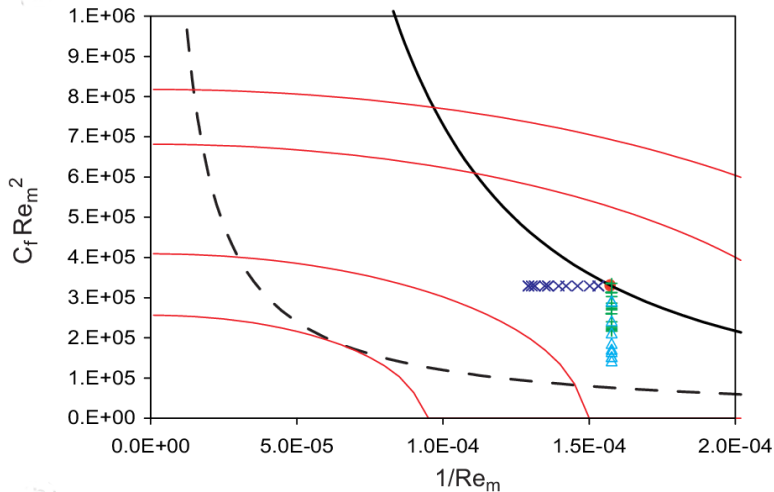
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# FURTHER RESULTS

SOW + STTW



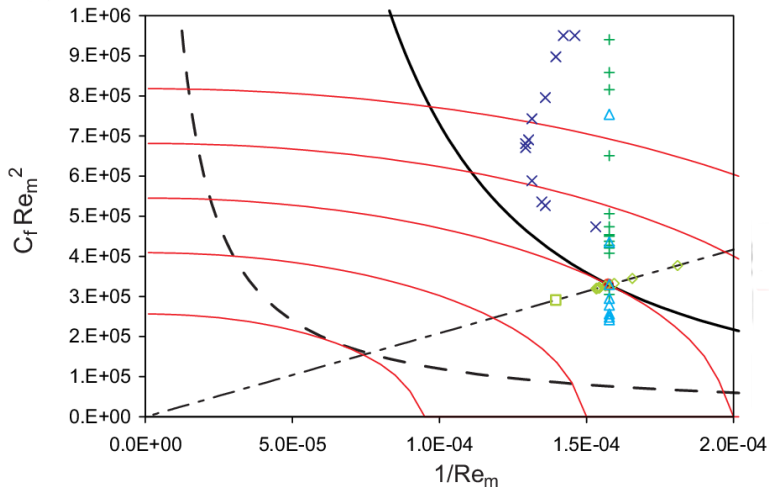
Background

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# FURTHER RESULTS

SOW + STTW



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# CONCLUSIONS

Background

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CPI

- Need to compromise between Money and Time
- Cost function is application-dependent
- CPI might be a useful alternative to CFR and CPG
- Our "application" is understanding physics

Reference: Frohnapfel, Hasegawa & Quadrio, "Money versus Time", JFM **700**, pp.406–418, 2012